

# Progress towards high resolution mass grid solutions from GRACE for global applications

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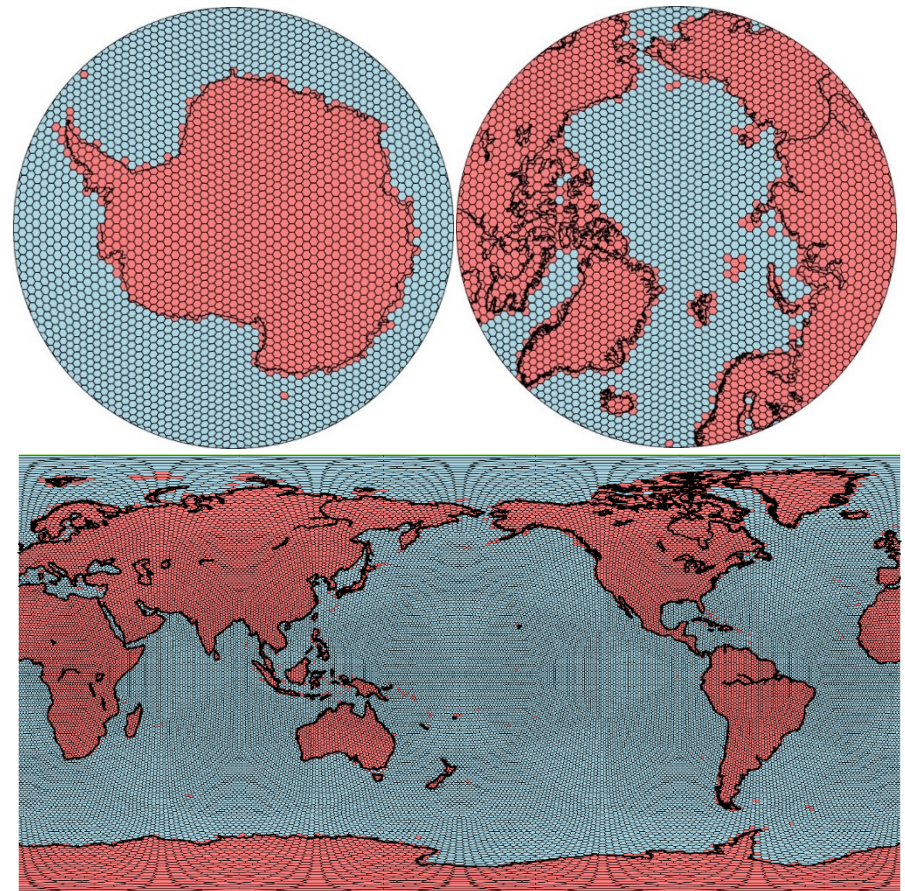
Center for Space Research

**GRACE Science Team Meeting, Austin TX, 2015**

# Geodesic Grid

- Geodesic grid technique\* used to model the surface of the earth
- Equal area gridded (approximate) representation of the earth
- 40962 Cells (40950 Hexagons + 12 Pentagons)
- Size of each cell is about equatorial  $1^\circ$
- Number of cells along the equator : 320
- Average area of each cell :  $12,400 \text{ km}^2$
- 120 km average distance between cell centers
- Does not suffer from over-sampling at the poles like equi-angular grid
- No single point of contact between neighboring cells

\* Ringler et. al., 1999



# Mass Grid inversion

Define a Transformation  $T$  to convert  $z$  (mass grid) to  $x$  (SHC)  $x = Tz$

Use  $R$  and  $b$  from the orthogonal transformation computed during SHC inversion setup

$$Rx = b \quad \text{Where, } QH = R \quad \text{and} \quad Qy = b$$

$$\text{Thus with } \bar{H}z = b \quad \text{Where, } \bar{H} = RT$$

Mass grid estimate can be computed using Tikhonov regularization as

$$\hat{z} = (\bar{H}^T \bar{H} + \mu M^T M)^{-1} \bar{H}^T b$$

The transformation matrix  $T$  is defined by discretizing the following integral equations over the defined grid

$$\Delta C_{jlm}(t) = \frac{\sigma_j(t)(1+k_j')R^2}{(2l+1)M} \int \bar{P}_{lm}(\sin \nu)(\cos m\lambda) d\Omega$$

$$\Delta S_{jlm}(t) = \frac{\sigma_j(t)(1+k_j')R^2}{(2l+1)M} \int \bar{P}_{lm}(\sin \nu)(\sin m\lambda) d\Omega$$

Where,  $\bar{P}_{lm}$  is Legendre associated polynomial,  $\sigma(t)$  is the mass of the layer over a unit of surface area at the epoch,  $t$ , for region,  $j$ ,  $k_j$  is the load love number,  $l$  is degree and  $m$  is order

# Tikhonov Regularization

$$\hat{z} = (\bar{H}^T \bar{H} + \mu M^T M)^{-1} \bar{H}^T b$$

GRACE information equations mapped into geodesic grid

GRACE observations

Regularization parameter

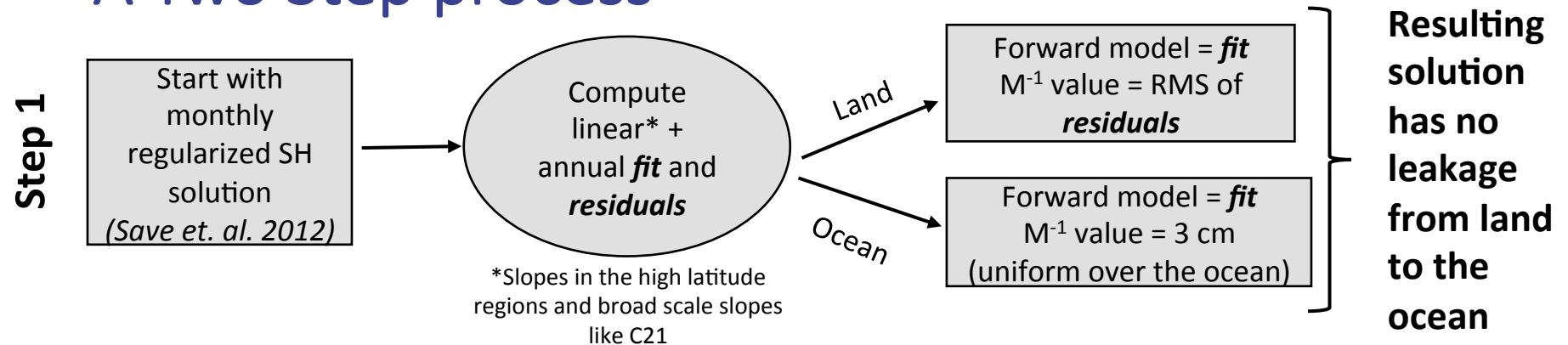
Regularization Matrix/Constraint Matrix

The diagram illustrates the components of the Tikhonov regularization equation. Arrows point from the text labels to the corresponding parts of the equation: 'GRACE information equations mapped into geodesic grid' points to  $\bar{H}^T \bar{H}$ , 'GRACE observations' points to  $b$ , 'Regularization parameter' points to  $\mu$ , and 'Regularization Matrix/Constraint Matrix' points to  $M^T M$ .

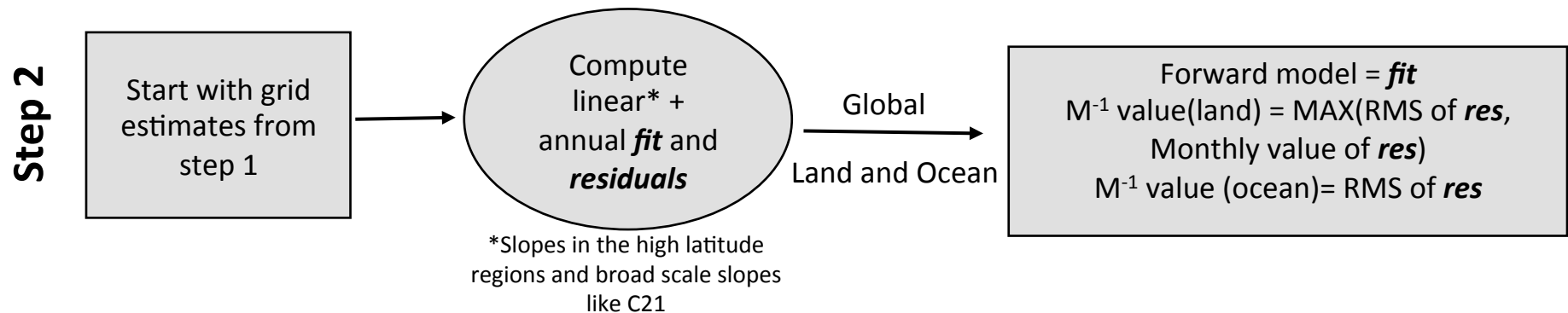
- Variable regularization matrix is designed for each monthly solution separately
- The regularization parameter is computed for each solution using L-curve method to balance the signal and noise in the solution\*

\* Described in Save et. at. 2012

# Regularization Matrix ( $M^{-1}$ ) Design: A Two Step process



Step 1 is only used to localize the GRACE signal to land areas

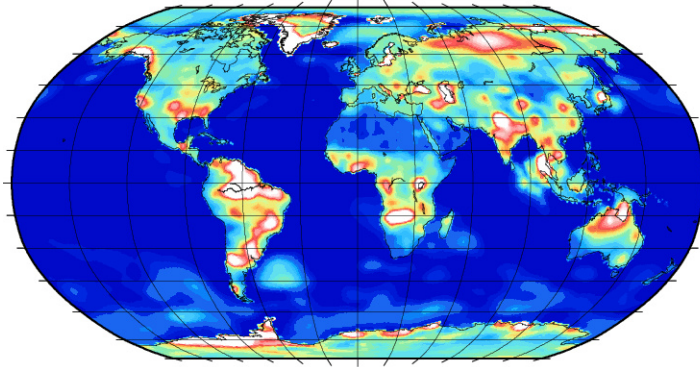


- The grid mass estimates are the correction to the linear + annual fit forward model
- linear + annual fit forward model is added back

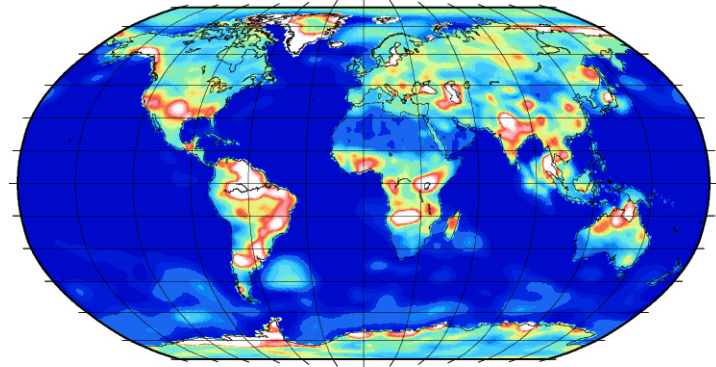


# Variable Regularization Matrix ( $M^{-1}$ )

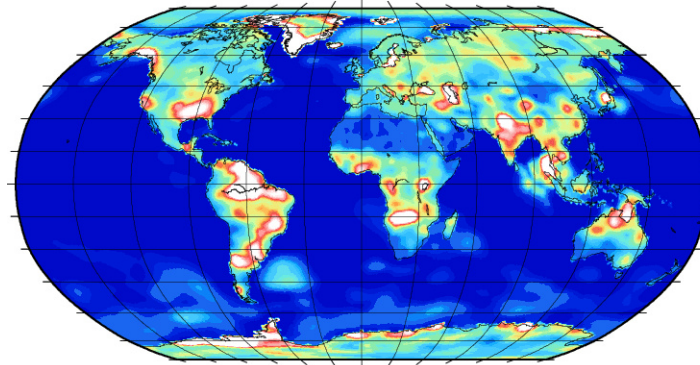
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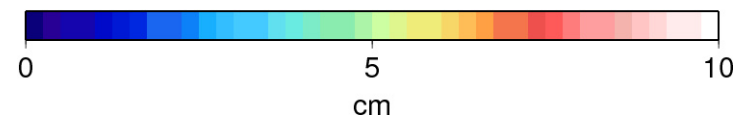
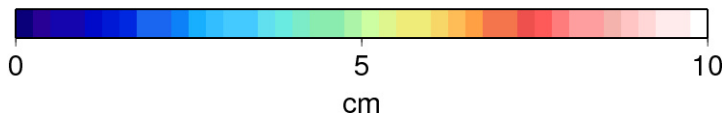
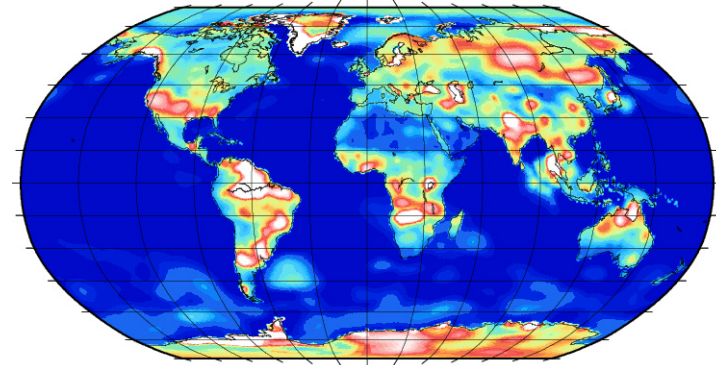
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Dec 2004



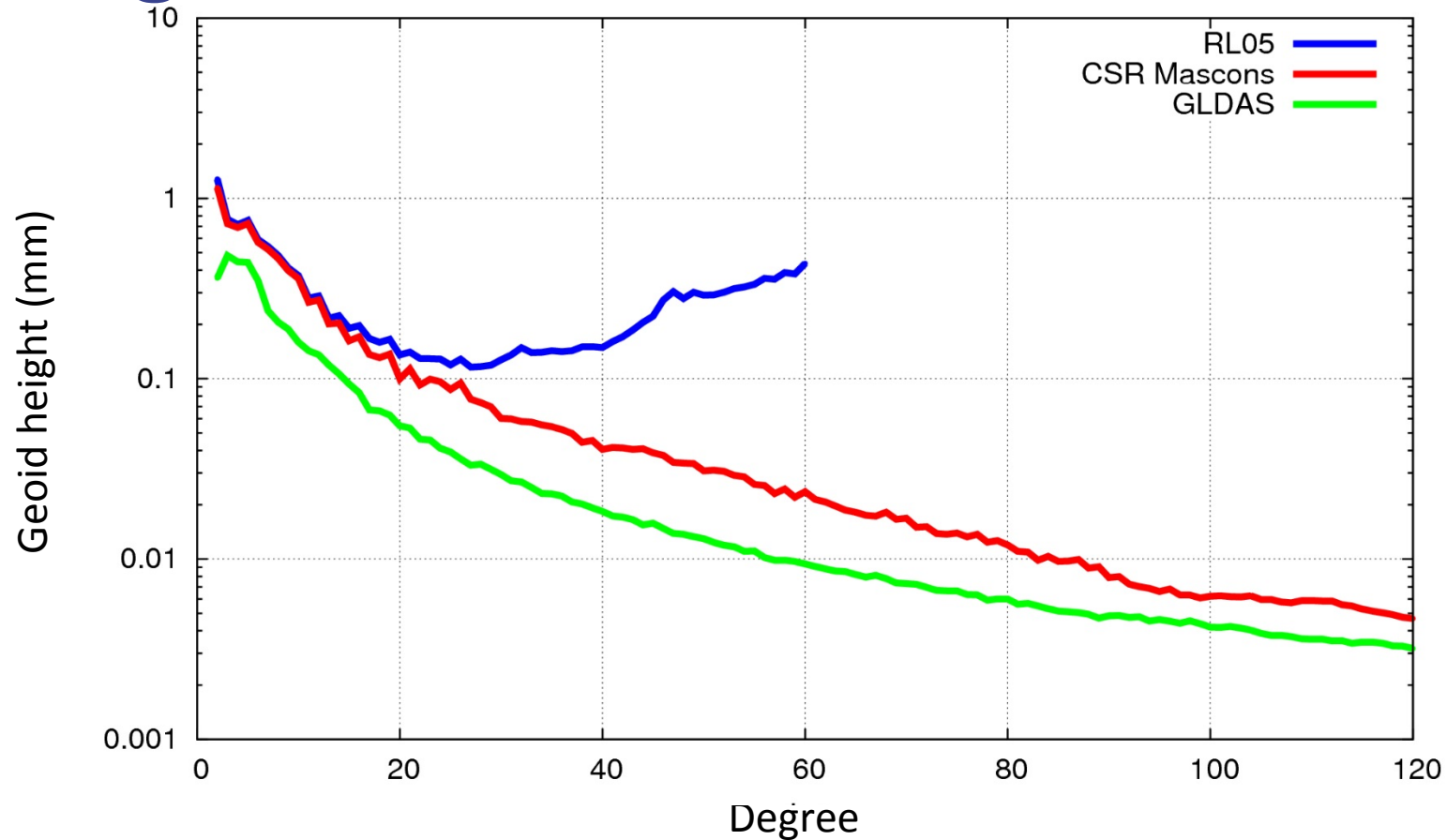
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# Regularization Matrix ( $M^{-1}$ )

- Regularization matrix is variable and is computed for each month independently
- No model information or independent data information was used to define the regularization matrix
- These global mascon solutions are purely driven by GRACE information without any influence from the hydrological/ocean models or other data
- Regularization Matrix is diagonal – No land/ocean correlations have been used

# Degree Variance

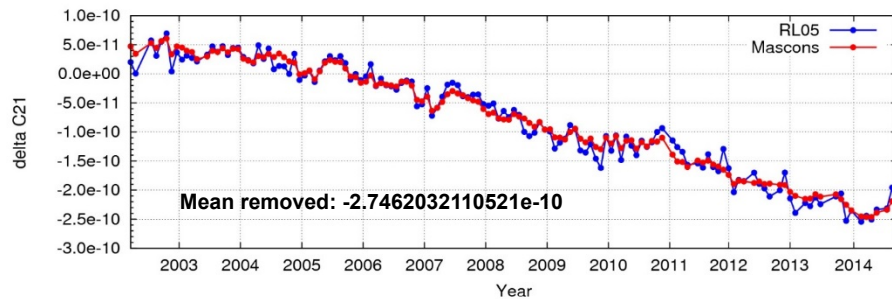


Degree Variance scatter shows that global mascon solutions capture all the low degree signal and deviate from RL05 solutions at degree 14

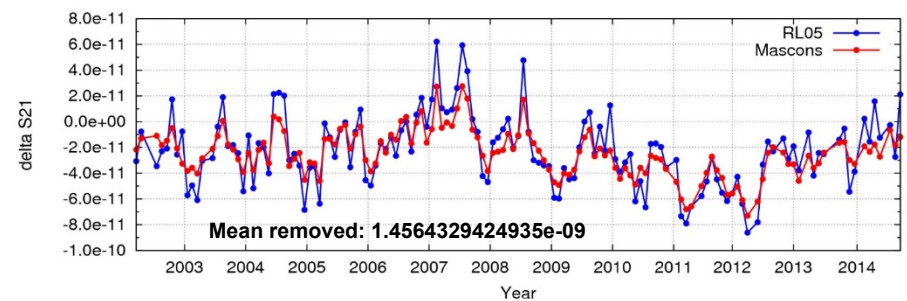


# Degree 2 Harmonics

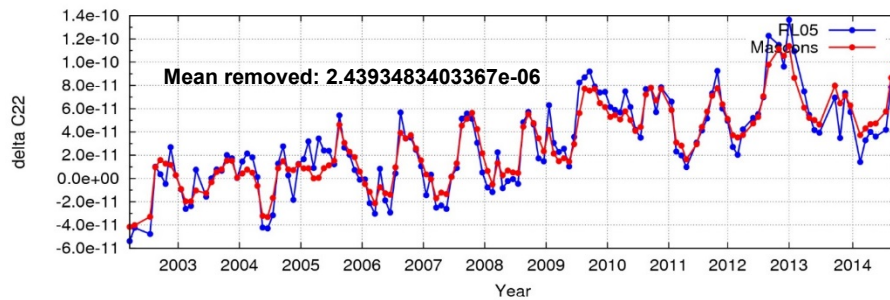
## C21



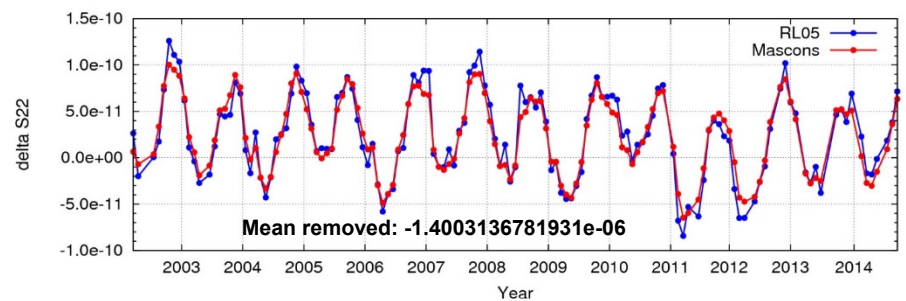
## S21



## C22

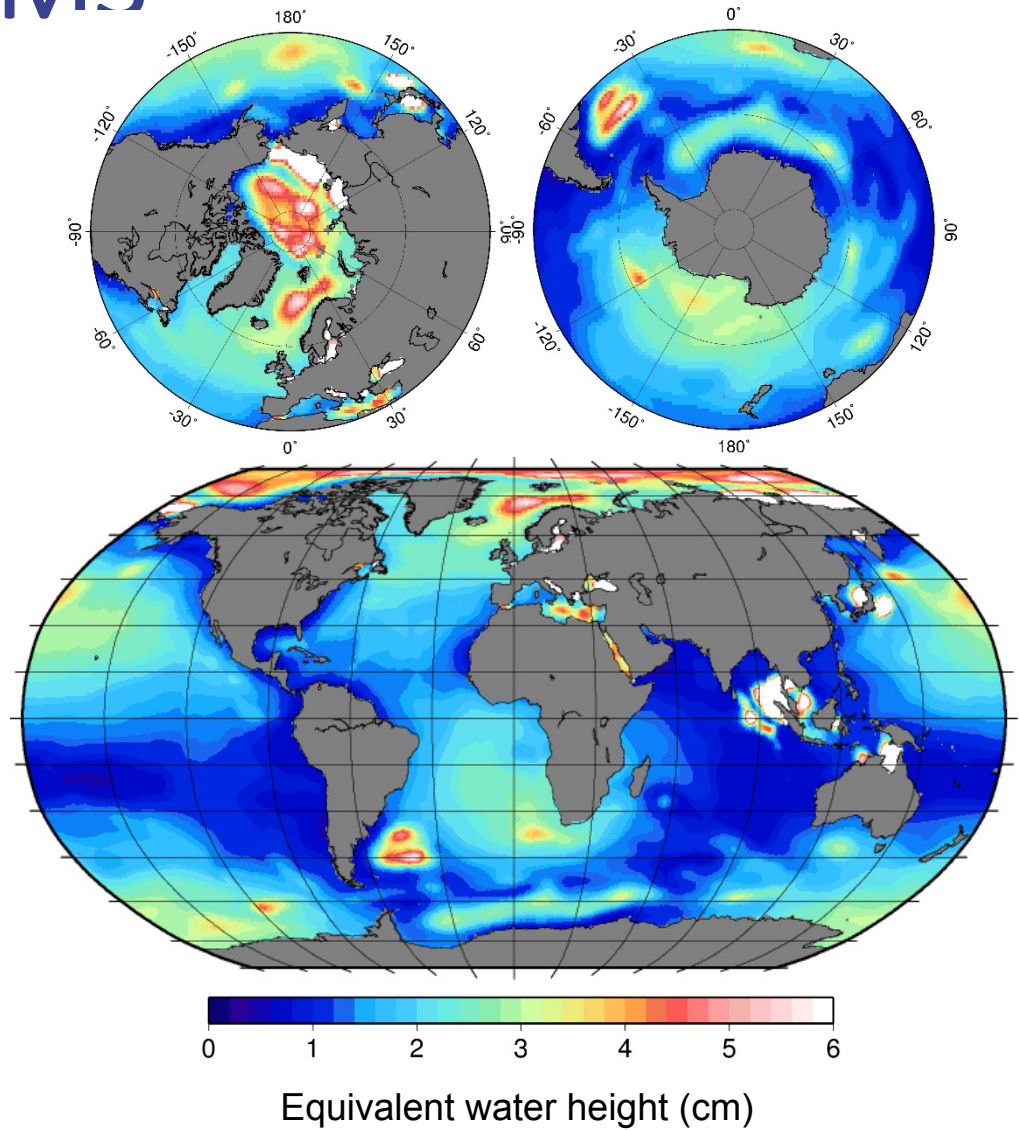


## S22



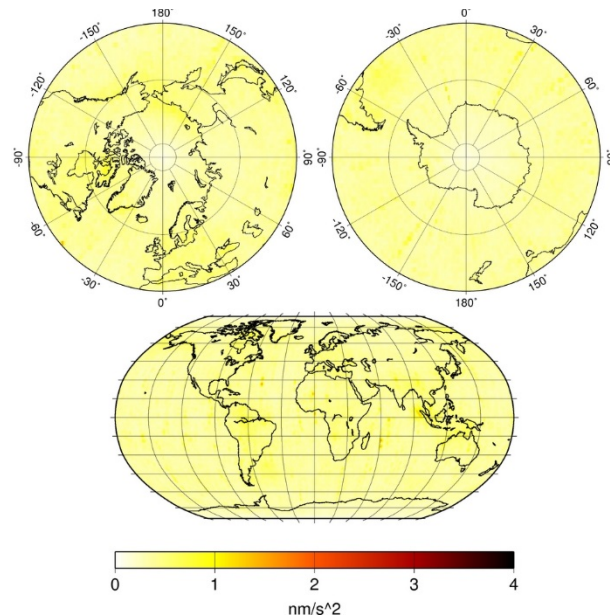
# Global Ocean RMS

Global RMS show significantly reduced noise over the ocean for the mass grid solutions. The corrections to the background de-aliasing model are in the expected regions.



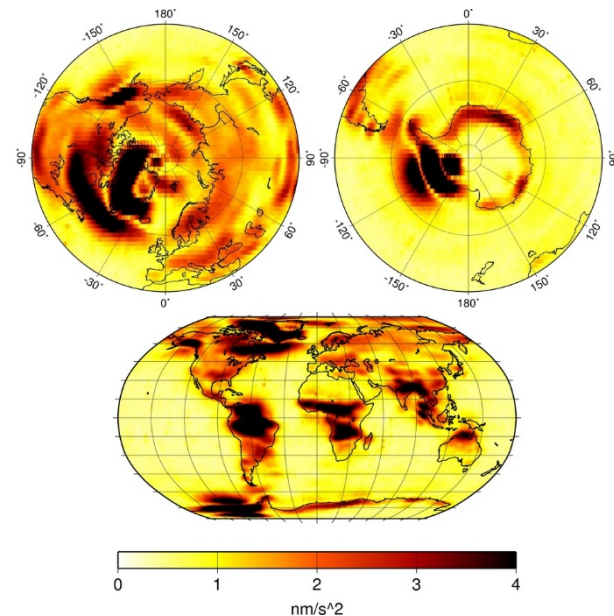
# Post-fit residual analysis

Residual range accelerations after fitting the GRACE range rate data to global mascon solutions (**post-fit**)



Min: 0.09633  $\text{nm/s}^2$ , Max: 2.04631  $\text{nm/s}^2$

Residual range accelerations of the full signal (**RL05 prefit**)

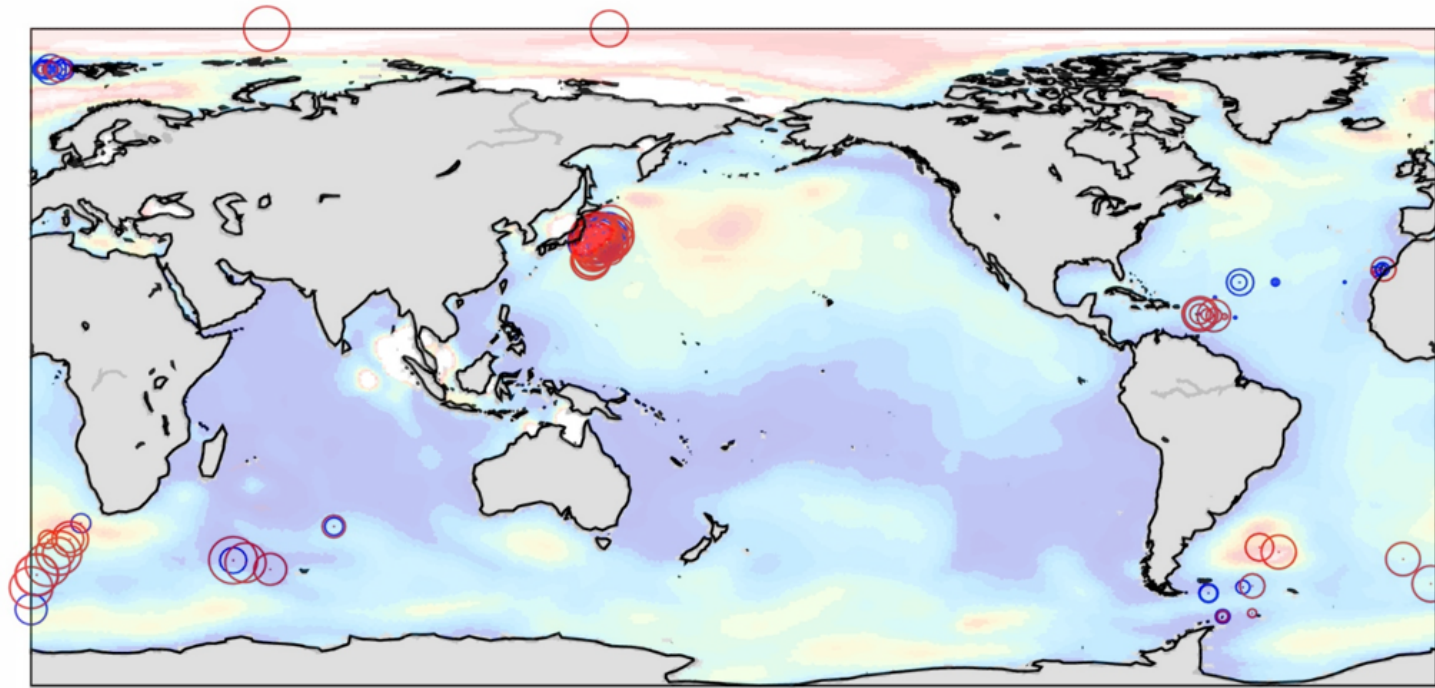


Min: 0.28076  $\text{nm/s}^2$ , Max: 24.4754  $\text{nm/s}^2$

**No geo-spatial correlation in the range-acceleration residuals**

The post-fit residuals are smaller than the GRACE errors of 3-4  $\text{nm/s}^2$ . The solutions meet the necessary condition and all the signal is captured in the solutions within the GRACE error levels

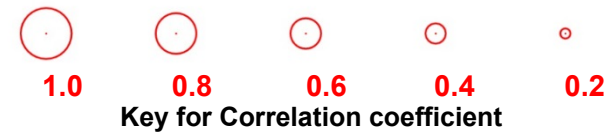
# Ocean Bottom Pressure Comparison



Background image is the RMS over the ocean of the mascon solutions.

Blue circle: OBPR corr w/ mascon+GAD < only GAD

Red circle: OBPR corr w/ mascon+GAD > only GAD



**Point wise comparison of the ocean bottom pressure recorder (OBPR)\* data and mascon cell mass estimate time series**

*\* Macrander et. al., 2010.*



# Ocean Bottom Pressure

Latitude	Longitude	Corr w/ JPL Mascons	Corr w/CSR Mascons
-50.25	1.42	0.85	0.75
47.66	4.26	0.81	0.83
-41.13	9.94	0.51	0.52
15.5	308.5	0.55	0.58
16.5	302.5	0.63	0.51
34.83	145.04	0.65	0.71
36.35	145.99	0.83	0.6
36.35	146.92	0.72	0.66
36.35	148.85	0.72	0.74
37.11	144.57	0.58	0.58
37.81	147.87	0.70	0.70
38.51	148.34	0.80	0.80
89.43	60.31	0.86	0.80

*Thanks to Carmen Boening for the OBPR comparisons*

# Comparison with published result

The mass anomaly computed in the Amundsen sea sector from CSR global mascon solutions, without any post processing, reproduces the results published by *Sutterly et. al., 2014*.

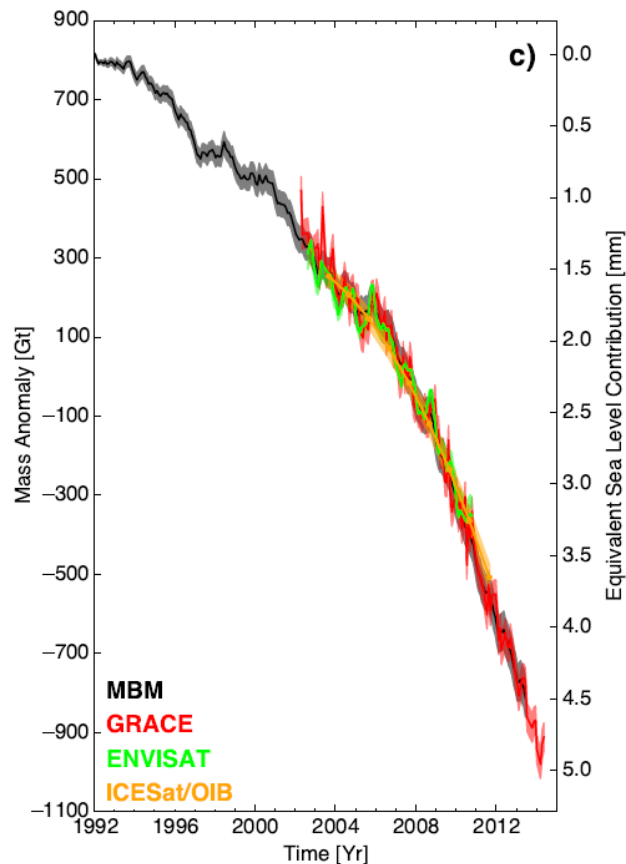
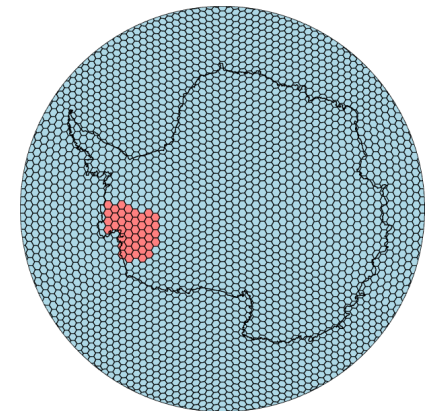
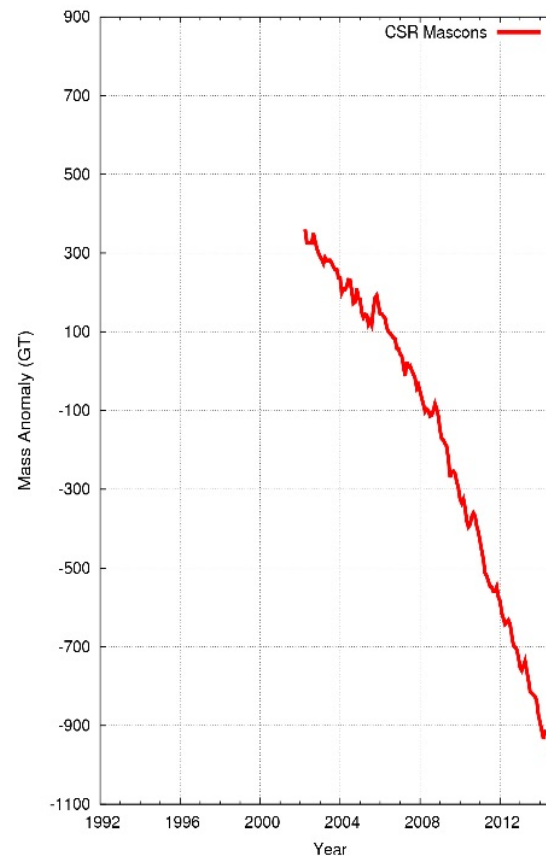


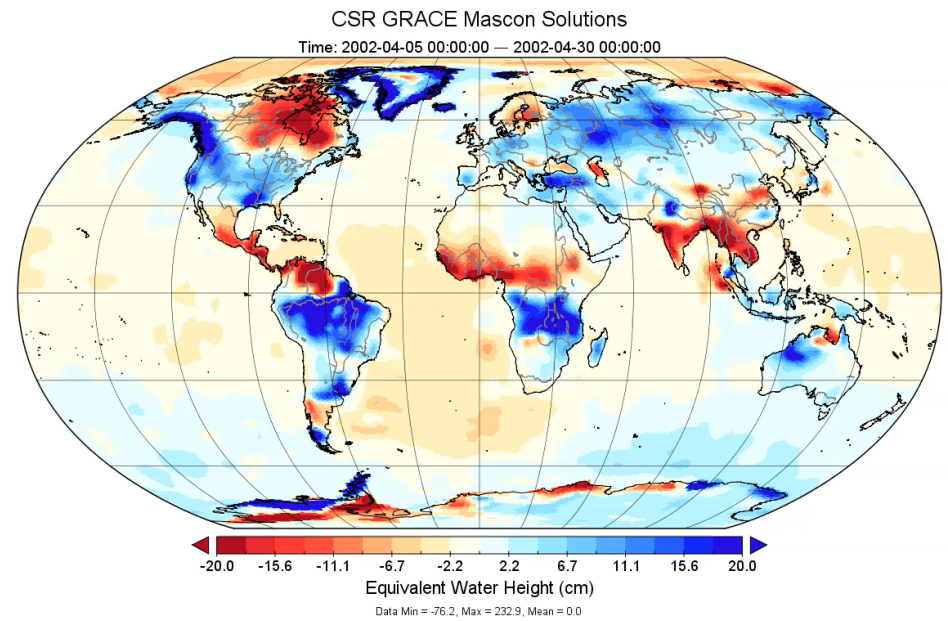
Image from Sutterley et. al. 2014





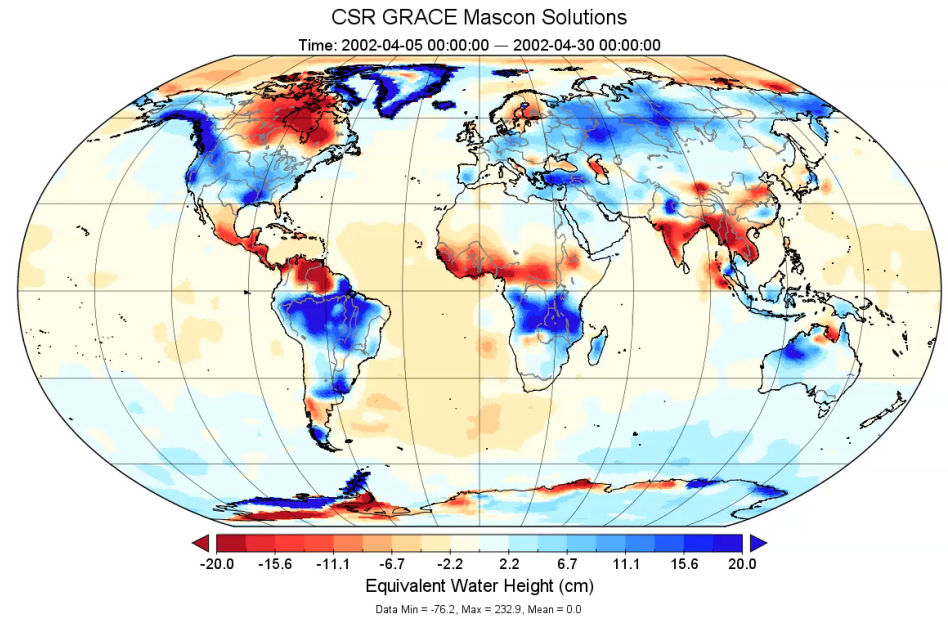
# CSR mascon solutions summary (1/2)

- The regularization is purely driven by GRACE and no model information is used in the computation.
- These solutions meet the necessary condition that the post-fit residuals show no geo-physical correlations and all the signal is captured within the noise level of GRACE.
- These solutions have excellent correlation with independent OBPR data.
- These solutions reproduce ice mass loss estimates without any need for post-processing.



# CSR mascon solutions summary (2/2)

- These solutions will be released to the user community soon.
  - C20 estimate will be replaced by the C20 estimate from SLR
  - Degree 1 component will be added
  - A GIA model will be removed
  - GAD will be added back for ocean applications
- Solutions will be available as 0.5° equi-angular grids
- No post-processing should be applied when using these solutions
- Single solution file will be available for use with global applications like Cryosphere, Oceanography and Hydrology etc.
- Please watch the space at <http://www.csr.utexas.edu/grace/> for upcoming release



# Thank you

Please contact  
Himanshu Save ([save@csr.utexas.edu](mailto:save@csr.utexas.edu))  
with any questions.

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